

Rate of return regulation

Numerical Problem with Welfare Analysis

This problem walks you through a numerical example demonstrating different outcomes possible for a natural monopoly. Be sure that you've read the relevant section of Viscusi, Henderson and Vernon Chapter 12 for a theoretical treatment of this topic. This problem is based on problem 3 at the end of that chapter.

Problem Setup

MetroPower Co. is a regulated electric utility.

The (inverse) market demand curve for electricity is

$$P = 50 - 0.25Q,$$

where P is the price per MWh and Q is the number of MWh sold.

Cost structure:

If the firm operates efficiently, its technology allows it to produce electricity at a constant marginal cost of \$20 per MWh. At that efficient input mix, average cost is also \$20 per MWh.

However, under rate-of-return regulation, the utility is allowed to earn an above-market return on capital. This creates an Averch–Johnson (A–J) distortion: the firm uses too much capital and does not minimize cost. As a result, under regulation its average cost rises to \$22 per MWh.

We will compare **three outcomes**:

1. Efficient competitive outcome (benchmark)

In a perfectly competitive, cost-minimizing industry:

- Price equals marginal cost.
- The firm uses the efficient input mix, so cost per unit is \$20.

Call this the *competitive outcome*:

$$P_C = 20.$$

Using the demand curve, find the competitive quantity Q_C .

Then compute:

- Consumer surplus CS_C
- Producer surplus PS_C (you can treat this as zero in long-run competitive equilibrium with constant cost)
- Total surplus TS_C

2. Unregulated monopoly

Now suppose MetroPower is an unregulated profit-maximizing monopolist. Assume it uses the *efficient* technology (so marginal cost is still \$20 per MWh).

For a linear demand curve

$$P = a - bQ,$$

marginal revenue is

$$MR = a - 2bQ.$$

For this market, that implies

$$MR = 50 - 0.5Q.$$

The monopoly chooses Q_M where $MR = MC$. Then it charges the price P_M from the demand curve.

Compute:

- Q_M, P_M
- Consumer surplus CS_M
- Producer surplus / profit PS_M
- Total surplus TS_M

Use cost \$20 per unit for profit.

3. Rate-of-return regulation with Averch–Johnson distortion

Suppose the regulator sets an allowed price such that the firm charges

$$P_R = 30$$

and sells

$$Q_R = 80.$$

However, because the firm is rewarded for capital spending, it uses too much capital. Its average cost rises to \$22 per MWh instead of \$20. Assume this \$22 is also the effective marginal cost under regulation.

Compute:

- Consumer surplus CS_R
- Producer surplus / profit PS_R
- Total surplus TS_R

Use $P_R = 30$, $Q_R = 80$, and per-unit cost \$22.

4. Graph and interpretation

On one graph:

- Put Q on the horizontal axis and P on the vertical axis.
- Draw the downward-sloping market demand curve

$$P = 50 - 0.25Q.$$

- Draw a horizontal line at $P = 20$ to represent marginal cost when the firm is efficient.
- (Optional but helpful) Draw a horizontal line at $P = 22$ to represent the higher, distorted cost under regulation with Averch–Johnson.

- Mark and label the three outcomes:

$$(Q_C, P_C) = (120, 20)$$

$$(Q_M, P_M) = (60, 35)$$

$$(Q_R, P_R) = (80, 30).$$

Then answer:

- (a) Relative to the competitive benchmark, how does the monopoly distort the market?
- (b) Relative to the competitive benchmark, how does the regulated firm with Averch–Johnson distortion distort the market?
- (c) Which outcome (monopoly or regulation) creates the higher total surplus? Briefly explain why.